



**GRÖBNER-SHIRSHOV BASES FOR THE WEYL  
GROUPS OF THE 3-EXTENDED AFFINE  
ROOT SYSTEMS OF TYPE  $A_1$**

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Received September 9, 2013

**Abstract**

We give Gröbner-Shirshov bases for the Weyl groups of the 3-extended affine root systems of types  $A_1^{(1,1,1)}$ ,  $A_1^{(1,1,1)*}(1)$ ,  $A_1^{(1,1,1)*}(2)$ ,  $A_1^{(1,1,1)*}(3)$ ,  $A_1^{(1,1,1)*}(4)$  and  $A_1^{(1,1,1)*}(5)$ .

**Pioneer Journal  
of Mathematics  
and Mathematical  
Sciences**



Pioneer Scientific  
Publisher

**Keywords and phrases:** Gröbner-Shirshov basis, Weyl group.