



GLOBAL EXISTENCE AND BLOW-UP TO A  $P$ -LAPLACIAN PARABOLIC SYSTEM WITH NONLINEAR MEMORY

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Abstract

This paper deals with a  $P$ -Laplacian parabolic system with nonlinear memory

$$u_t - \operatorname{div}(|\nabla u|^{p-2}\nabla u) = u^m \int_0^t v^\alpha ds$$

$$v_t - \operatorname{div}(|\nabla v|^{q-2}\nabla v) = v^n \int_0^t u^\beta ds$$

with homogeneous Dirichlet boundary conditions in a bounded domain  $\Omega \subset R^N$ , where  $p, q > 2, \alpha, \beta, m, n \geq 1$ . Under appropriate hypotheses, we obtain that the solution either exists globally or blows up in finite time.

**Keywords and phrases:**  $P$ -Laplacian, quasilinear degenerate parabolic system, blow up, global existence, nonlinear memory.

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